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Method and arrangement for controlling injection of reducing agent**FIELD OF THE INVENTION, AND STATE OF THE ART**

- 10 The present invention relates to a method and a device for controlling the injection of reducing agent upstream from a catalyst in an exhaust line from a combustion engine. The invention also relates to a computer program comprising program codes for implementation of said method, a computer program product comprising a medium which is readable by an electronic control unit and has stored on it a computer program intended to cause an electronic unit to implement said method, and an electronic control unit.
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- 20 To meet prevailing exhaust cleaning requirements, today's motor vehicles are usually provided with a catalyst in the exhaust line for effecting catalytic conversion of environmentally harmful components of exhaust gases to environmentally less harmful substances. One method employed for achieving effective
- 25 catalytic conversion is based on injection of a reducing agent in the exhaust gases upstream from the catalyst. A reducing substance forming part of or formed by the reducing agent is carried by the exhaust gases into the catalyst, in which it is adsorbed on active seats in the catalyst, thereby causing storage
- 30 (accumulation) of the reducing substance in the catalyst. The stored reducing substance may either desorb, i.e. become detached from the active seats, or react with an exhaust gas substance so as to convert said exhaust gas substance to a harmless substance. Such a reduction catalyst may for example
- 35 be of SCR type (SCR = Selective Catalytic Reduction). This type of catalyst is hereinafter called SCR catalyst. An SCR catalyst selectively reduces NO_x in exhaust gases but not the oxygen in

exhaust gases. In the case of an SCR catalyst, a reducing agent in the form of urea or ammonia is usually injected in the exhaust gases upstream from the catalyst. Injection of urea into exhaust gases results in the formation of ammonia and it is this ammonia
5 that constitutes the reducing substance which assists the catalytic conversion in the SCR catalyst. The ammonia is accumulated in the catalyst by being adsorbed on active seats in the catalyst, and NO_x present in the exhaust gases is converted to nitrogen and water by being brought into contact with ammonia
10 accumulated on active seats in the catalyst.

When a reduction catalyst is used in combination with proportioning of reducing agent, it is important to control the injection of the reducing agent so that desired conversion of the
15 exhaust gas substance concerned is achieved without allowing excessive amounts of unconsumed reducing substance to accompany the exhaust gases leaving the catalyst and thereby reach the environment. The consumption of reducing agent and the relating costs can thereby be minimised while at the same
20 time preventing or at least minimising undesired release of the reducing substance to the environment. The fact, for example, that ammonia is a reducing substance which is toxic and malodorous makes it desirable to minimise to the utmost possible extent the release of this ammonia to the environment while
25 maintaining the injection of sufficient reducing agent, e.g. in the form of urea, for achieving the required conversion of the exhaust gas substance concerned, in this case NO_x.

When a catalyst of the type here concerned is used, the injection
30 of reducing agent is at the present time usually controlled on the basis of two-dimensional tables, each of which is related to a certain exhaust gas temperature. Each table comprises values for the amount of reducing agent to be injected in the exhaust line at the respective load and speed of the combustion engine concerned. Each table thus has engine load on a first axis and engine speed on a second axis. These tables are compiled
35 empirically by charting the behaviour of the respective

combustion engine and catalyst on the basis of performance in steady-state conditions. Such charting has to be done for each specific combination of combustion engine and catalyst, and this previously known solution also involves extensive trial runs and

5 settings for each specific combination of engine type and catalyst type. Any changes in, for example, engine emissions entail having to make extensive and detailed changes to all the values in the tables. As the tables give proportioning adapted to steady-state conditions, dynamic compensations have to be applied in

10 cases where operating conditions change quickly. A further disadvantage of the known solution is that, despite dynamic compensations, operating conditions for which the tables do not cater can occur, which may lead to incorrect proportioning of reducing agent.

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OBJECT OF THE INVENTION

The object of the present invention is to provide a method which enables easy and reliable control of the injection of reducing

20 agent upstream from a catalyst in an exhaust line from a combustion engine so that amounts of reducing agent which are appropriate to prevailing operating conditions can be injected.

SUMMARY OF THE INVENTION

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According to the invention, said object is achieved by means of a method exhibiting the features indicated in claim 1.

The solution according to the invention involves:

30 - an accumulation actual value representative of current accumulation in the catalyst of a reducing substance forming part of or formed by the reducing agent being calculated on the basis of information from a computation model which, taking into account the reactions in the catalyst under prevailing operating

35 conditions, continuously determines the current state of the catalyst, e.g. the accumulation of the reducing substance in

- different parts of the catalyst and the conversion of exhaust gas substance taking place in different parts of the catalyst,
- an accumulation setpoint value being calculated on the basis of an emission setpoint value and information from said
- 5 computation model, whereby the emission setpoint value is representative of a desired content, in the exhaust gases leaving the catalyst, of an exhaust gas substance which, as the exhaust gases pass through the catalyst, is at least partly removed from the exhaust gases by the action of the reducing substance or is
- 10 formed by the action of the reducing substance, and the accumulation setpoint value is representative of the accumulation of the reducing substance which is required in the catalyst under prevailing operating conditions for substantially achieving the emission setpoint value,
- 15 - the accumulation actual value being compared with the accumulation setpoint value, and
- the injection of reducing agent in the exhaust line being controlled on the basis of the result of the comparison between the accumulation actual value and the accumulation setpoint
- 20 value.

The solution according to the invention makes it possible easily and reliably to control the injection of reducing agent upstream from a catalyst in an exhaust line from a combustion engine so

25 that suitable amounts of reducing agent can be injected, based on prevailing operating conditions, for achieving a desired conversion of the exhaust gas substance concerned. Taking the current reducing substance accumulation in the catalyst into account makes it possible to control the proportioning of reducing

30 agent with good accuracy so that the desired conversion of the exhaust gas substance is accomplished while at the same time the amount of unconsumed reducing substance which accompanies the exhaust gases leaving the catalyst and thereby reaches the environment is limited. It thus becomes possible to

35 minimise the consumption of reducing agent and the relating costs while at the same time preventing or at least minimising undesired release of reducing agent to the environment. The

computation model used need only be adapted to the catalyst and is therefore independent of the design of the combustion engine connected to the catalyst. Using a computation model which is only tied to the catalyst and not to the combustion

5 engine results in a very flexible method which, when adapted to a specific catalyst, can be used for that catalyst together with any desired combustion engine. It is also possible to use a scalable computation model which can easily be adapted to the dimensions of the catalyst.

10 According to an embodiment of the method according to the invention, a limitation factor is calculated, which limitation factor has a value based on an estimate of the current risk that the reducing substance content of the exhaust gases leaving the
15 catalyst might exceed a predetermined limit value, whereby this limitation factor is taken into account in calculating the accumulation setpoint value in such a way that the accumulation setpoint value decreases in response to increasing risk that the reducing substance content of the exhaust gases leaving the
20 catalyst might exceed the predetermined limit value. It thus becomes possible to eliminate or at least minimise the risk that undesired amounts of unconsumed reducing substance might accompany the exhaust gases leaving the catalyst and thereby reach the environment.

25 A further embodiment of the method according to the invention is characterised by:
- an emission actual value being established by calculation or measurement, which emission actual value is representative of
30 the current content of the exhaust gas substance in the exhaust gases leaving the catalyst,
- the emission actual value being compared with the emission setpoint value, and
- the accumulation setpoint value being calculated on the basis
35 of information from said computation model and the conformity between the emission actual value and the emission setpoint value.

The fact of thus causing the conformity between the emission actual value and the emission setpoint value to affect the accumulation setpoint value makes it possible to calculate the accumulation setpoint value by an approximation method, since
5 the influence on the accumulation setpoint value of the conformity between the emission actual value and the emission setpoint value makes it possible to compensate for deviations arising between desired and actual emissions of the exhaust gas substance. The calculated accumulation setpoint value thus
10 need not correspond exactly to the reducing substance accumulation required for achieving the emission setpoint value.

Further embodiments of the method according to the invention are indicated by the dependent claims and the description set out
15 below.

The invention also relates to a device according to claim 21 for utilising the method according to the invention.

- 20 The invention also relates to a data program according to claim 23 which is loadable directly to the internal memory of a computer and which comprises program codes for implementation of the method according to the invention.
- 25 The invention also relates to a computer program product according to claim 24 comprising a medium which is readable by an electronic control unit and which has stored on it a computer program intended to cause an electronic control unit to implement the method according to the invention.
- 30 The invention also relates to an electronic control unit according to claim 25.

BRIEF DESCRIPTION OF THE DRAWINGS

The invention is described in more detail below on the basis of examples of embodiments with reference to the attached drawings, which are as follows:

- 5 Fig. 1 a schematic diagram of a combustion engine with a relating catalyst and a device according to the invention,
- 10 Fig. 2 a block diagram illustrating a first embodiment of the device according to the invention,
- Fig. 3 a block diagram illustrating a second embodiment of the device according to the invention,
- 15 Fig. 4 a block diagram illustrating an electronic control unit for implementation of the method according to the invention,
- 20 Fig. 5 a flowchart illustrating a method according to a first embodiment of the present invention,
- Fig. 6 a flowchart illustrating a method according to a second embodiment of the present invention,
- 25 Fig. 7 a flowchart illustrating a method according to a third embodiment of the present invention, and
- 30 Fig. 8 a flowchart illustrating a method according to a fourth embodiment of the present invention, and
- Fig. 9 a flowchart illustrating a method according to a fifth embodiment of the present invention.

DETAILED DESCRIPTION OF EMBODIMENTS

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Fig. 1 depicts schematically a combustion engine 1 provided with a device 10 according to the invention. The exhaust gases

leaving the combustion engine 1 pass through an exhaust line 2 and reach the environment via an exhaust outlet 3. A reduction catalyst 4, preferably in the form of an SCR catalyst, is arranged in the exhaust line 2. The exhaust gases from the combustion
5 engine 1 are thus caused to pass through this catalyst 4 before reaching the environment via the exhaust outlet 3. An injection point 5 for reducing agent is situated in the exhaust line 2 upstream from the catalyst 4. The injection of reducing agent takes place via an injection device comprising one or more
0 injection means 6 arranged in the exhaust line, in the form of injection nozzles or the like, and a reducing agent storage tank 7 connected thereto. The injection device further comprises a proportioning unit 8, which itself comprises proportioning means and a regulating means, e.g. a control valve or the like, arranged
5 to regulate the supply of reducing agent to said injection means
6. The proportioning unit 8 is controlled by a device 10 according to the present invention which determines the amount of reducing agent to be injected in the exhaust gases.

?0 Fig. 2 illustrates a first embodiment of a device 10 according to the invention. The device 10 comprises a first calculation means
20 adapted to determining continuously, by use of a computation model, the current state of the catalyst, taking into account the expected reactions in the catalyst under prevailing operating
25 conditions. The computation model takes into account the expected exothermal and endothermal reactions in the catalyst 4 under prevailing operating conditions and calculates inter alia the accumulation of the reducing substance concerned in different parts of the catalyst, and the conversion of the exhaust gas
30 substance concerned which takes place in different parts of the catalyst. The computation model may be of any desired design provided that it produces with the desired accuracy a correct value for the accumulation of the reducing substance and the conversion of the exhaust gas substance in the catalyst. An
35 example of a computation model suitable in the context is described below.

The device 10 further comprises a second calculation means 30 adapted to calculating, on the basis of information from the first computation means 20, an accumulation actual value A_1 representative of the current accumulation in the catalyst 4 of the

5 reducing substance which forms part of or is formed by the reducing agent. The second computation means 30 is also adapted to calculating an accumulation setpoint value A_2 on the basis of an emission setpoint value E_2 and information from said computation model. This emission setpoint value E_2 is

10 representative of a desired content, in the exhaust gases leaving the catalyst 4, of an exhaust gas substance which, as the exhaust gases pass through the catalyst, is at least partly removed from the exhaust gases by the action of the reducing substance or is formed by the action of the reducing substance.

15 The emission setpoint value E_2 provides a measure of the maximum permissible emission of the exhaust gas substance and may inter alia be controlled by statutory exhaust emission requirements. The emission setpoint value E_2 has in the simplest case a constant value but is preferably determined by

20 calculation in a computation means 38 in a conventional manner on the basis of prevailing operating conditions, e.g. the speed and load of the combustion engine. The accumulation setpoint value A_2 is representative of the reducing substance accumulation required in the catalyst under prevailing operating

25 conditions for achieving or at least substantially achieving the emission setpoint value E_2 . The first computation means 20 and the second computation means 30 are with advantage integrated in a common computer unit but may, if considered appropriate, take the form of separate units connected to one another.

30 The device 10 further comprises a comparator 32 adapted to receiving the accumulation actual value A_1 and the accumulation setpoint value A_2 from the second computation means 30. The comparator 32 is adapted to comparing the accumulation actual

35 value A_1 and the accumulation setpoint value A_2 and to emitting a signal S_1 which depends on the conformity, e.g. the difference, between this actual value A_1 and setpoint value A_2 . The device

10 also comprises regulating means 34, 36 for controlling the injection of reducing agent on the basis of said signal S1 from the comparator 32. Said regulating means comprise with advantage a regulator 34, preferably in the form of a PI regulator or PID regulator, adapted to receiving the signal S1 from the comparator 32. On the basis of that signal S1, the regulator 34 emits a control signal S2 to a control means 36 connected to the proportioning unit 8 of the injection device and adapted to controlling this proportioning unit on the basis of said control signal S2 so that an amount of reducing agent appropriate to prevailing conditions is injected in the exhaust line 2.

The control signal S2 from the regulator 34 may also be led to the first computation means 20 in order to be used in the computation model, as a measure of the amount of reducing agent injected, when generating information for the next calculation of accumulation actual value A1 and accumulation setpoint value A2. Alternatively, the first computation means 20 may be adapted to receiving from the control means 36 a value representing the amount of reducing agent injected, as illustrated in Fig. 3.

Fig. 3 illustrates a second embodiment of a device 10 according to the invention. The components which appear both in the embodiment described above with reference to Fig. 2 and in the embodiment according to Fig. 3 are denoted by the same reference notations. In the embodiment according to Fig. 3, the device 10 likewise comprises means for determining by calculation or measurement an emission actual value E1 representative of the current exhaust gas substance content of the exhaust gases leaving the catalyst 4. In cases where the emission actual value E1 is determined by calculation, this is preferably done in the first computation means 20 by using the abovementioned computation model or in a separate computation means on the basis of information from that computation model. In cases where the emission actual value E1 is determined by

measurement, this is done by a measuring means arranged in the exhaust line downstream from the catalyst 4.

In the embodiment according to Fig. 3, the second computation
5 means 30 is adapted to calculating the accumulation setpoint
value A_2 on the basis of information from the first computation
means 20 and the conformity between the emission actual value
 E_1 and the emission setpoint value E_2 . In this case the device
10 comprises a comparator 42 adapted to receiving the emission
actual value E_1 and the emission setpoint value E_2 . The
comparator 42 is adapted to comparing the emission actual value
 E_1 and the emission setpoint value E_2 and to emitting a signal
 S_3 which depends on the conformity, e.g. the difference,
between this actual value E_1 and setpoint value E_2 . The device
15 10 comprises with advantage a regulator 44, preferably in the
form of a PI regulator or PID regulator, which is adapted to
receiving the signal S_3 from the comparator 42. On the basis of
that signal S_3 the regulator 44 emits a control signal f_{SP} to the
second computation means 30, which then determines the
20 accumulation setpoint value A_2 on the basis of that control signal
 f_{SP} and the information from the first computation means 20 so
that the accumulation setpoint value A_2 is to the necessary
extent compensated for undesired deviations between the
emission actual value E_1 and the emission setpoint value E_2 .

25 In the embodiment according to Fig. 3, regulation is applied in
the form of so-called cascade regulation whereby the second
computation means 30, the comparator 32 and the regulator 34
constitute an inner regulating circuit 12a which sets a necessary
30 reducing substance accumulation in the catalyst by acting upon
the proportioning of the reducing agent, and whereby the
comparator 42 and the regulator 44 constitute an outer regulating
circuit 12b which sets a desired emission of the exhaust gas
substance by acting, via the inner regulating circuit 12a, upon the
35 level of the necessary accumulation of the reducing substance in
the catalyst.

Program codes for implementation of the method according to the invention are preferably adapted to forming part of a computer program directly loadable to the internal memory of a computer, e.g. to the internal memory of the aforesaid computer unit. Such

5 a computer program is provided with advantage via a computer program product comprising a storage medium which is readable by a computer and on which the computer program is stored. Said storage medium takes the form, for example, of an optical storage medium in the form of a CD-ROM disc, a DVD disc etc.,

10 or of a magnetic storage medium in the form of a hard disc, a diskette, a cassette tape etc. Fig. 4 illustrates an electronic control unit 50 comprising a means 51, preferably a central processor unit (CPU), for execution of software, which communicates via a databus 52 with a memory 53, e.g. of the

15 RAM type. The control unit 50 also comprises at least one storage medium 54, e.g. in the form of a memory of the ROM, PROM, EPROM or EEPROM type or a Flash memory, which the execution means 51 communicates with via the databus 52. A computer program comprising program codes for implementation

20 of the method according to the invention is stored in the storage medium 54.

The reducing agent preferably takes the form of urea ($\text{CO}(\text{NH}_2)_2$) but may also take the form of, for example, ammonia (NH_3) or

25 hydrocarbon (fuel). In the ensuing description it is assumed that the catalyst 4 is an SCR catalyst and that a reducing agent in the form of urea or ammonia is used. It should be noted, however, that the solution according to the invention is not limited to this type of reduction catalyst and this type of reducing agent.

30 Injecting urea into exhaust gases results in the formation of ammonia and it is this ammonia that constitutes the reducing substance which assists the catalytic conversion in the SCR catalyst. In this case the exhaust gas substance concerned takes the form of NO_x .

35 The aforesaid computation model is with advantage designed to use the following parameters as input values:

a) The exhaust gas temperature P_1 upstream from the catalyst 4. This temperature may be determined by temperature sensor or in any of the conventional ways of calculating it.

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b) The NO_x concentration P_2 in the exhaust gases upstream from the catalyst 4. This concentration may be determined by sensor but is determined with advantage in any of the conventional ways of calculating it, e.g. on the basis of the combustion engine's load, speed, injection angle, i.e. the angle of the combustion engine's crankshaft at the time of fuel injection into the engine cylinders, and, where applicable, the EGR content (EGR = Exhaust Gas Recirculation), i.e. the content of exhaust gases led back to the engine.

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c) The exhaust gas mass flow P_3 through the catalyst 4. This exhaust gas mass flow may be determined by mass flow sensor but is determined with advantage in any of the conventional ways for calculating it, e.g. on the basis of the combustion engine's load and speed.

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d) The amount P_4 of reducing agent injected in the exhaust gases. The value for the amount of reducing agent injected is obtained with advantage from the control means 36 or from the regulator 34.

The computation model may also use as input value the O_2 concentration in the exhaust gases upstream from the SCR catalyst and/or the ambient temperature. The O_2 concentration

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may be determined by, for example, lambda sensor but is determined with advantage in any of the conventional ways for calculating it, e.g. on the basis of the combustion engine's load, speed and, where applicable, EGR content.

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A design of computation model is described below which it is advantageous to use for obtaining information for calculating the aforesaid accumulation actual value A_1 , accumulation setpoint

value A2 and, where applicable, emission actual value E1 which pertain to a method and a device according to the present invention.

- 5 In an SCR catalyst, nitrogen oxide NO_x reacts with ammonia and is reduced to nitrogen gas. NO_x is the harmful exhaust gas substance intended to be removed from the exhaust gases, and ammonia is the reducing substance used for achieving this.
- 10 Ammonia or urea (which converts to ammonia) is injected in the exhaust gases upstream from the SCR catalyst. The computation model is used to determine how much NO_x is converted in the SCR catalyst and how much unconsumed ammonia leaves the SCR catalyst. The computation model also calculates continuously how the temperature varies across the
- 15 catalyst and how much ammonia is accumulated in different parts of the catalyst. This involves the computation model being continuously supplied with information about the magnitude of the gas flow through the catalyst and the temperature and composition of the gas flowing into the catalyst.

20 A number of reactions take place in the SCR catalyst. Ammonia is adsorbed on active seats in the catalyst, resulting in accumulation of ammonia in the catalyst. The accumulated ammonia may either desorb, i.e. become detached from the

25 active seats, or react with NO_x . At high temperatures, oxidation of ammonia with oxygen also takes place to a certain extent. The factor which decides how much NO_x is converted in the catalyst is the reaction velocities r_i of the various reactions. The reactions and their relating reaction velocities are as follows:

- 30
- 1) $\text{S} + \text{NH}_3 \rightarrow \text{S.NH}_3 \quad r_1 = k_1 c_{\text{NH}_3} \theta_v$
 - 2) $\text{S.NH}_3 \rightarrow \text{S} + \text{NH}_3 \quad r_2 = k_2 \theta_{\text{NH}_3}$
 - 35 3) $4\text{S.NH}_3 + 4\text{NO} + \text{O}_2 \rightarrow 4\text{S} + 4\text{N}_2 + 6\text{H}_2\text{O} \quad r_3 = k_3 c_{\text{NO}} \theta_{\text{NH}_3}$
 - 4) $4\text{S.NH}_3 + 5\text{O}_2 \rightarrow 4\text{S} + 6\text{H}_2\text{O} + 4\text{NO} \quad r_4 = k_4 c_{\text{O}_2} \theta_{\text{NH}_3}$

where k_i is the velocity constant for reaction i , c_i is the concentration of substance i , θ_V is the proportion of vacant seats, and θ_{NH_3} is the proportion of seats occupied by ammonia. The 5 reaction velocities r_i are temperature-dependent in accordance with the Arrhenius equation:

$$k_i = k_{0,i} e^{-\frac{E_{A,i}}{RT}}$$

10 where $k_{0,i}$ is constant for reaction i , $E_{A,i}$ is the activation energy for reaction i , R is the general gas constant, and T is the temperature.

To determine the composition of the exhaust gases after the 15 catalyst and how much ammonia is accumulated in different parts of the SCR catalyst, a number of material balances are solved according to the computation model. As the SCR catalyst has a monolithic structure, the gas flows through small channels whereby the walls between the channels contain the active 20 catalyst material. The catalyst is modelled by regarding the flow through a channel as divided into a number of segments. The material balances are solved successively from the segment at the catalyst's inlet to the segment at the catalyst's outlet. From the flow through the channel, NO_x and ammonia are transported 25 up to the wall of the duct, where these substances react. To take into account the effect of the velocity at which the substances are transported up to the channel wall and into the channel wall, the channel wall is likewise divided into a number of segments. As all the material balances in the wall segments within each 30 channel segment are inter-related, they have to be solved together in an equation system. According to the computation model, the following material balances are set up:

$$F_{tot}(y_{i,k-1} - y_{i,k}) - \Gamma_{i,k,0}(c_{i,k,0} - c_{i,k,1}) = 0$$

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$$\Gamma_{i,k,n-1}(c_{i,k,n-1} - c_{i,k,n}) - \Gamma_{i,k,n}(c_{i,k,n} - c_{i,k,n+1}) + \sum_j v_{i,j} r_{j,k,n} w_{k,n} = 0 \quad \text{for } n \geq 1$$

where F_{tot} is the total molar flow, $y_{i,k}$ and $c_{i,k}$ are the molar proportion and the concentration respectively of substance i in channel segment k , $\Gamma_{i,k,0}$ and $\Gamma_{i,k,n}$ are the respective coefficients

- 5 for transport of substance i from the gas flow to the first wall segment and between wall segments n and $n+1$ in channel segment k , $v_{i,j}$ are stoichiometric coefficients for substance i in reaction j , $r_{j,k,n}$ is the reaction velocity for reaction j in channel segment k and wall segment n , and $w_{k,n}$ is the mass of active catalyst material in channel segment k and wall segment n . The ammonia accumulation in channel segment k and wall segment n is then arrived at by the material balance:

$$N_c \frac{d\theta_{NH_3,k,n}}{dt} = \sum_j v_{i,j} r_{j,k,n}$$

- 15 where N_c is the number of active seats per unit mass of catalyst.

- To determine the temperature across the SCR catalyst, a heat balance for the gas and a heat balance for the catalyst are solved according to the computation model in a similar manner.
- 20 The heat balance for the gas is given by:

$$F_{tot} c_p (T_{g,k-1} - T_{g,k}) - h_k A_k (T_{g,k} - T_{s,k}) = 0$$

- 25 where $T_{g,k}$ and $T_{s,k}$ are the gas temperature and catalyst temperature respectively in channel segment k , c_p is the thermal capacity of the gas, h_k is the heat transfer coefficient in channel segment k , and A_k is the wall area in channel segment k . The heat balance for the catalyst is given by:

$$m_{s,k} c_{p,s} \frac{dT_{s,k}}{dt} = h_k A_{k,0} (T_{g,k} - T_{s,k}) + \sum_n \sum_j r_{j,k,n} w_{k,n} (-\Delta H_j)$$

where $m_{s,k}$ is the mass of catalyst in channel segment k , $c_{p,s}$ is the thermal capacity of the catalyst material, and $-\Delta H_j$ is the reaction heat for reaction j .

- 5 As a specialist in the field will appreciate, the computation model indicated above may be modified in many different ways and it is also possible to use a type of computation model other than that indicated above in order to obtain required information for calculating the accumulation actual value $A1$, the accumulation
- 10 setpoint value $A2$ and, where applicable, the emission actual value $E1$.

Figs. 5-9 depict flowcharts illustrating the method according to various embodiments of the present invention. The method steps illustrated in Figs. 5-9 are effected continuously when the catalyst 4 and the relating injection device are active. As a first step, the current state of the catalyst is calculated by means of a computation model of the type indicated above. Information obtained by the calculations in the computation model is thereafter used for calculating the aforesaid accumulation actual value $A1$ and accumulation setpoint value $A2$. The accumulation actual value $A1$ and accumulation setpoint value $A2$ are then compared and on the basis of this comparison a control signal $S2$ for proportioning of reducing agent is generated. As a final step, proportioning and injection of reducing agent in the exhaust line are effected on the basis of said control signal $S2$. The amount of reducing agent injected is thus controlled on the basis of the conformity between the accumulation actual value $A1$ and the accumulation setpoint value $A2$.

According to the embodiment illustrated in Fig. 5, an emission setpoint value $E2$ of the type described above is determined, whereby this emission setpoint value $E2$ is taken into account in calculating the accumulation setpoint value $A2$.

An emission setpoint value $E2$ is also determined in the embodiment illustrated in Fig 6. In this embodiment, an emission actual value $E1$ of the type indicated above is likewise calculated on the basis of information from the computation model. This

- 5 emission actual value $E1$ is compared with the emission setpoint value $E2$ and this comparison serves as the basis for generating a control signal f_{sp} which is then taken into account in calculating the accumulation setpoint value $A2$. The calculation of the accumulation setpoint value $A2$ is thus affected by the conformity
10 between the emission actual value $E1$ and the emission setpoint value $E2$.

In the embodiment illustrated in Fig. 7, a limitation factor $f_{constrain}$ is calculated on the basis of information from the computation

- 15 model, which limitation factor has a value which depends on an estimate of the current risk that the reducing substance content of the exhaust gases leaving the catalyst might exceed a predetermined limit value. This limitation factor $f_{constrain}$ is then taken into account in calculating the accumulation setpoint value
20 $A2$ in such a way that the accumulation setpoint value $A2$ decreases in response to increasing risk that the reducing substance content of the exhaust gases leaving the catalyst might exceed the predetermined limit value. The limitation factor $f_{constrain}$ is used with advantage as a multiplication factor in
25 calculating the accumulation setpoint value $A2$, and to this end it is given a value which ranges between 0 and 1 depending on the current risk that the reducing substance content of the exhaust gases leaving the catalyst might exceed the predetermined limit value, whereby the value of the limitation factor is close to 1
30 when there is no such risk and close to 0 when such risk is imminent. In this embodiment, a control signal f_{sp} of the type described above is likewise taken into account in calculating the accumulation setpoint value $A2$.

- 35 In the embodiment illustrated in Fig. 8, the accumulation setpoint value $A2$ is calculated by multiplication of two multiplication factors, whereby a first multiplication factor takes the form of a

calculated accumulation maximum value A_{max} representative of the maximum permissible reducing substance accumulation in the catalyst under prevailing operating conditions, and a second multiplication factor f_{sp} depends on the conformity between the
5 emission actual value $E1$ and the emission setpoint value $E2$. Said second multiplication factor corresponds to the control signal f_{sp} indicated above. The accumulation maximum value A_{max} is calculated on the basis of information from the computation model. Here again it is advantageous to calculate a
10 limitation factor $f_{constrain}$ of the type indicated above, whereby this limitation factor $f_{constrain}$ is taken into account in calculating the accumulation maximum value A_{max} in such a way that the accumulation maximum value A_{max} decreases in response to increasing risk that the reducing substance content of the
15 exhaust gases leaving the catalyst might exceed the predetermined limit value.

Maximum permissible reducing substance accumulation in the catalyst means here the greatest reducing substance
20 accumulation which, according to calculations performed, can be permitted in the catalyst under prevailing operating conditions without the release of unconsumed reducing substance to the environment exceeding the limit value determined.

25 In the embodiment illustrated in Fig. 9, a limit value profile $\theta_{NH_3,k}^L$ is calculated for the ammonia accumulation along the catalyst, which is then used for determining the catalyst's capacity for NO_x conversion under prevailing operating conditions. The NO_x conversion capacity determined is used in calculating the
30 accumulation setpoint value $A2$, thereby making it possible to act upon the accumulation setpoint value $A2$ in such a way as to reduce the risk that the reducing substance content of the exhaust gases leaving the catalyst might exceed a predetermined limit value. It thus becomes possible to eliminate or at least
35 minimise the risk that undesired amounts of unconsumed reducing substance might accompany the exhaust gases leaving the catalyst and thereby reach the environment, without any

limitation factor of the type indicated above having to be used. A disadvantage associated with using the previously described limitation factor is that inertia and great non-linearity of regulation occur in cases where the limitation factor changes

5 from low to high value or from high to low value. The embodiment according to Fig. 9 is not subject to any such disadvantage and enables linear regulation with very good performance.

10 In a simplified variant, the method according to the invention may be so designed that the accumulation actual value A_1 and the accumulation setpoint value A_2 refer respectively to the current and required reducing substance accumulation in the computation model's catalyst segment situated nearest to the

15 inlet end of the catalyst, i.e. nearest to the latter's upstream end. In this case, the accumulation actual value A_1 can be obtained directly from the computation model, and the accumulation setpoint value A_2 may for example be obtained by the calculation algorithm set out below, according to which the catalyst is

20 divided in its longitudinal direction into a multiplicity of segments in a manner corresponding to the computation model indicated above. The calculation algorithm used for determining the accumulation setpoint value A_2 and the accumulation actual value A_1 is hereinafter called the proportioning algorithm.

25 The first thing to determine is a limit value profile for the mole fraction of reducing substance through the catalyst:

$$y_{R,k}^L = y_{L,R} + y_{NO_x,k} - y_{NO_x,K}$$

30 where $y_{L,R}$ is the limit value for the mole fraction of reducing substance leaving the catalyst, and $y_{NO_x,k}$ and $y_{NO_x,K}$ are the respective mole fractions of NO_x in segments k and K (K = the last segment of the catalyst). As the mole fraction for NO_x

35 decreases along the catalyst, the mole fraction for reducing substance in the limit value profile will likewise decrease along the catalyst. The limit value profile for the mole fraction of

reducing substance is then used for calculating a limit value profile for accumulation of reducing substance:

$$\theta_{R,k}^L = \frac{K(T_{s,k}) \cdot c_{tot,k} \cdot y_{R,k}^L}{1 + K(T_{s,k}) \cdot c_{tot,k} \cdot y_{R,k}^L}$$

5

where $K(T_{s,k})$ is the equilibrium constant for adsorption of reducing substance at the temperature T_s in segment k , and $c_{tot,k}$ is the total gas concentration. The equilibrium constant is determined by the ratio between the respective velocity constants $k_a(T_{s,k})$ and $k_d(T_{s,k})$ for adsorption and desorption of reducing substance:

$$K(T_{s,k}) = \frac{k_a(T_{s,k})}{k_d(T_{s,k})}$$

- 15 The ratio between complete NO_x conversion and current NO_x conversion is determined by:

$$f_{max} = \frac{y_{NO_x,0}}{y_{NO_x,0} - y_{NO_x,k}}$$

- 20 This ratio is used for determining the profile for the mole fraction of reducing substance in the case of complete NO_x conversion:

$$y_{R,k}^{max} = y_{L,R} + f_{max} (y_{NO_x,k} - y_{NO_x,K})$$

- 25 This profile is then used for determining a corresponding reducing substance accumulation profile:

$$\theta_{R,k}^{max} = \frac{K(T_{s,k}) \cdot c_{tot,k} \cdot y_{R,k}^{max}}{1 + K(T_{s,k}) \cdot c_{tot,k} \cdot y_{R,k}^{max}}$$

- 30 Desorption velocities are calculated both for current reducing substance accumulation and for the limit value of reducing substance accumulation:

$$r_{d,k} = k_d(T_{s,k})\theta_{R,k}$$

$$r_{d,k}^L = k_d(T_{s,k})\theta_{R,k}^L$$

5

Thereafter, the ratio between these velocities is calculated:

$$f_{d,k} = \frac{r_{d,k}}{r_{d,k}^L}$$

10 The ratio is used for determining a limitation factor:

$$f_{constrain} = \frac{1}{1 + (c_1^{tune} f_{d,a} + c_2^{tune} f_{d,b})^{c_3^{tune}}}$$

where segments *a* and *b* and the parameters c_1^{tune} , c_2^{tune} and c_3^{tune}

15 can respectively be selected and trimmed in order to achieve optimum functioning. The limitation factor has the characteristics of being close to unity when the accumulation of reducing substance is small relative to the accumulation limit value. When the accumulation is close to the limit value, the value of the
20 limitation factor decreases. The accumulation setpoint value A2 is finally determined by:

$$A2 = A_{max} \cdot f_{SP} = \theta_{R,1}^{\max} \cdot f_{constrain} \cdot f_{SP}$$

25 where f_{SP} is the control signal from the outer regulating circuit 12b. Here it may be seen that the limitation factor affects the accumulation setpoint value A2. When the reducing substance accumulation is close to the limit value, the accumulation setpoint value A2 will thus decrease until a state of equilibrium
30 obtains. In this case the accumulation actual value A1 is the accumulation of reducing substance in the first segment of the catalyst:

$$A1 = \theta_{R,1}$$

In the proportioning algorithm formulae set out above, R denotes the current reducing substance. In cases where the reducing substance takes the form of ammonia, R therefore stands for
5 NH_3 .

With this simple variant of the proportioning algorithm it is possible to achieve rapid regulation of the accumulation of the reducing substance in the catalyst. As it is the reducing
10 substance accumulation in the catalyst's first segment that is regulated, the response to changes in proportioning of reducing agent is rapid. It is also possible to trim the regulation so that the amount of reducing substance leaving the catalyst without reacting is constantly below the limit value, since a limitation
15 factor lowers the accumulation setpoint value A_2 when the accumulation of reducing substance is close to the limit value. The principal disadvantage of this simple proportioning algorithm variant is that the internal control state, i.e. the reducing substance accumulation in the catalyst, is not directly
20 representative of the NO_x conversion in the catalyst. As the NO_x conversion is temperature-dependent, more accumulation at lower temperatures is required for achieving the same NO_x conversion. This means that it is the outer regulating circuit 12b that has to compensate the accumulation setpoint value A_2 in
25 response to temperature changes. Another problem is that temperature changes cause the temperature along the catalyst to vary and the reducing substance to be consumed at different rates in different parts of the catalyst. As the internal control state is only related to the first segment of the catalyst, the
30 variations across the catalyst have to be compensated by the outer regulating circuit 12b.

In a more refined variant, the method according to the invention may be so designed:

35 - that for each of the segments of the computation model an accumulation actual value A_k and a conversion value $R_{\max,k}$ are calculated, whereby the accumulation actual value A_k is

representative of the maximum reducing substance accumulation in the segment which is permitted under prevailing operating conditions, and the conversion value $R_{max,k}$ is representative of the expected exhaust gas substance conversion in the segment

- 5 when the reducing substance accumulation in the segment corresponds to the accumulation value A_k ,
 - that the conversion values $R_{max,k}$ for the various segments are summated, and
 - that the resulting sum is converted to a fictitious value for the
- 10 maximum permissible reducing substance accumulation in the segment situated nearest to the inlet end of the catalyst, whereby this fictitious value constitutes the aforesaid accumulation maximum value A_{max} .

- 15 The accumulation maximum value A_{max} thus obtained then serves as the basis for arriving at the accumulation setpoint value $A2$ in the manner indicated above by multiplication by a multiplication factor f_{sp} which depends on the conformity between the emission actual value $E1$ and the emission setpoint value $E2$.

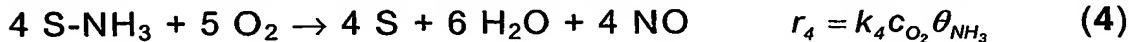
- 20 A limitation factor $f_{constrain,k}$ of the type described above is with advantage calculated for each of the segments, whereby this limitation factor $f_{constrain,k}$ is taken into account in calculating the conversion values $R_{max,k}$ in such a way that the conversion values decrease in response to increasing risk that the reducing substance content of the exhaust gases leaving the catalyst might exceed the predetermined limit value.

- 30 A value R_k for the current conversion of the exhaust gas substance in the segment is further calculated for each of the segments. A value R_{tot} for the total current conversion of the exhaust gas substance in the catalyst is then calculated by summating the values R_k of the various segments, followed by converting the value R_{tot} thus obtained for the total current conversion of the exhaust gas substance in the catalyst to a fictitious value for the current reducing substance accumulation in the segment situated nearest to the inlet end of the catalyst,

whereby this fictitious value constitutes the accumulation actual value A1.

In this refined variant, the internal control state provides a

- 5 representative measure of the NO_x conversion through the whole catalyst. In this case the proportioning algorithm will be related to how the computation model for the catalyst is formulated. The following example illustrates how the proportioning algorithm might be designed if the reducing substance is ammonia and the 10 computation model for the catalyst comprises the following reactions with relating reaction velocities:



The reaction velocities are given per unit mass of catalyst.

- 20 Summating the reaction velocity for reaction 3 (NO_x conversion) multiplied by the catalyst mass in the respective segments, and then dividing the result by the expression for the reaction velocity in the first segment multiplied by the catalyst mass but with the accumulation of ammonia omitted, provides a measure of the 25 NO_x conversion through the whole catalyst, expressed in ammonia accumulation for the first segment in the catalyst, which constitutes the current value of the internal control state, i.e. the accumulation actual value A1:

$$A1 = \Phi_{NH_3} = \frac{\sum_{k=1}^K k_3(T_{s,k}) \cdot c_{tot,k} \cdot y_{NOx,k} \cdot \theta_{NH_3,k} \cdot w_k}{k_3(T_{s,1}) \cdot c_{tot,1} \cdot y_{NOx,k} \cdot w_1}$$

30 The setpoint value for the internal control state, i.e. the accumulation setpoint value A2, is determined in a similar manner:

$$A2 = \Phi_{SP,NH_3} = f_{SP} \cdot \frac{\sum_{k=1}^K f_{constrain,k} \cdot k_3(T_{s,k}) \cdot c_{tot,k} \cdot y_{NOx,k} \cdot \theta_{NH_3,k}^{\max} \cdot w_k}{k_3(T_{s,1}) \cdot c_{tot,1} \cdot y_{NOx,k} \cdot w_1}$$

where $\theta_{NH_3,k}^{\max}$ may be determined in the same way as $\theta_{R,k}^{\max}$ in the proportioning algorithm described above in the simplified variant of the method according to the invention. The limitation factors may be given different values for each segment according to:

$$f_{constrain,k} = \frac{1}{1 + c_k^{tune} \cdot f_{d,k}}$$

- 10 where $f_{d,k}$ is determined in the same manner as in the proportioning algorithm described above in the simplified variant of the method according to the invention, and where the parameter c_k^{tune} may be trimmed differently for each segment.
- 15 This refined variant has the same advantages as the simplified variant. It is possible to achieve rapid regulation of the internal control state, since the latter is closely related to the reducing substance accumulation in the first segment of the catalyst. The proportioning algorithm can also be trimmed so that the amount of reducing substance leaving the catalyst without reacting is constantly below the limit value, since the limitation factors lower the accumulation setpoint value A2 when the reducing substance accumulation is close to the limit value. In contrast to the simplified variant, the internal control state in the refined
- 20 proportioning algorithm is related to the NO_x conversion. This means that the accumulation setpoint value A2 is automatically adjusted when the temperature changes. The fact that the internal control state is related to the NO_x conversion through the whole catalyst means that the proportioning algorithm is also able to compensate for varying consumption of reducing substance in different parts of the catalyst, caused by temperature variations along the catalyst. The refined proportioning algorithm is thus able to compensate for most of the variations which may occur along the catalyst, which means
- 25
- 30

that the outer regulating circuit 12b need only make minor adjustments to the accumulation setpoint value A2 in order to hold the NO_x emission at a desired level.

- 5 A possible implementation of the embodiment according to Fig. 9 is described in more detail below on the basis that the reducing substance is ammonia, whereby the computation model for the catalyst comprises the following reactions with relating reaction velocities:

10



- 15 Information from the catalyst model is used for estimating the NO_x conversion capacity of the catalyst. Surface concentration factors η for NO_x and ammonia are calculated as follows:

$$\eta_{NO_x,k} = \frac{y_{NO_x,k,s}}{y_{NO_x,k,g}}$$

20

$$\eta_{NH_3,k} = \frac{y_{NH_3,k,s}}{y_{NH_3,k,g}}$$

where $y_{NO_x,k,s}$ and $y_{NO_x,k,g}$ are the respective NO_x mole fractions on the internal wall surface and in the gas flow in channel

- 25 segment k, and $y_{NH_3,k,s}$ and $y_{NH_3,k,g}$ are the respective NH₃ mole fractions on the internal wall surface and in the gas flow in channel segment k. The denominators are monitored if they are nil and in such cases the surface concentration factor is set at 1, i.e.:

30

$$y_{NO_x,k,g} = 0 \Rightarrow \eta_{NO_x,k} = 1$$

$$y_{NH_3,k,g} = 0 \Rightarrow \eta_{NH_3,k} = 1$$

An ammonia concentration factor $f_{NH_3,k}$ is calculated as follows:

$$f_{NH_3,k} = \frac{y_{NH_3,k,g}}{y_{NH_3,k,g} + 2 \cdot y_{Urea,k,g}}$$

- 5 where $y_{Urea,k,g}$ is the mole fraction of urea in the gas flow in channel segment k.

An iterative procedure is used thereafter for determining the limit value profile $\theta_{NH_3,k}^L$ for the ammonia accumulation along the

- 10 catalyst. In the first iteration, the derivative for the molar limit value fraction of NO_x relative to the molar limit value fraction of ammonia is set at an initial value:

$$\left[\frac{dy_{NO_x}^L}{dy_{NH_3}^L} \right]^1 = -0.5$$

15

In the subsequent iterations, this derivative is calculated as follows:

$$\frac{dy_{NO_x}^L}{d\theta_{NH_3}^L} = - \frac{y_{NO_x,1} \cdot \theta_{NH_3,1} \cdot y_{NO_x,0} (y_{NO_x,0} - y_{NO_x,1})}{(\theta_{NH_3,1}^L (y_{NO_x,0} - y_{NO_x,1}) + y_{NO_x,1} \cdot \theta_{NH_3,1})^2}$$

20

$$\frac{d\theta_{NH_3}^L}{dy_{NH_3}^L} = \frac{k_1(T_{s,1}) \cdot c_{tot,1} \cdot \eta_{NH_3,1} (k_2(T_{s,1}) + v_3 \cdot k_3(T_{s,1}) \cdot c_{tot,1} \cdot y_{NO_x,1}^L \cdot \eta_{NO_x,1})}{(k_1(T_{s,1}) \cdot c_{tot,1} \cdot y_{NH_3,1}^L \cdot \eta_{NH_3,1} + k_2(T_{s,1}) + v_3 \cdot k_3(T_{s,1}) \cdot c_{tot,1} \cdot y_{NO_x,1}^L \cdot \eta_{NO_x,1})^2}$$

$$\left[\frac{dy_{NO_x}^L}{dy_{NH_3}^L} \right]^{update} = \begin{cases} -1 & \frac{dy_{NO_x}^L}{d\theta_{NH_3}^L} \cdot \frac{d\theta_{NH_3}^L}{dy_{NH_3}^L} \leq -1 \\ \frac{dy_{NO_x}^L}{d\theta_{NH_3}^L} \cdot \frac{d\theta_{NH_3}^L}{dy_{NH_3}^L} & -1 < \frac{dy_{NO_x}^L}{d\theta_{NH_3}^L} \cdot \frac{d\theta_{NH_3}^L}{dy_{NH_3}^L} < 0 \\ 0 & \frac{dy_{NO_x}^L}{d\theta_{NH_3}^L} \cdot \frac{d\theta_{NH_3}^L}{dy_{NH_3}^L} \geq 0 \end{cases}$$

25

$$\left[\frac{dy_{NO_x}^L}{dy_{NH_3}^L} \right]^i = f^i \cdot \left[\frac{dy_{NO_x}^L}{dy_{NH_3}^L} \right]^{i-1} + (1 - f^i) \cdot \left[\frac{dy_{NO_x}^L}{dy_{NH_3}^L} \right]^{update}$$

In each iteration the following calculations are also done:

$$5 \quad f^{L,update} = \frac{y_{NO_x,0} - y_{NO_x,1} - \left[\frac{dy_{NO_x}^L}{dy_{NH_3}^L} \right]^i \cdot (2y_{L,NH_3} + y_{NO_x,1} - y_{NO_x,K})}{y_{NO_x,0} - y_{NO_x,1} + \left[\frac{dy_{NO_x}^L}{dy_{NH_3}^L} \right]^i \cdot (y_{NO_x,1} - y_{NO_x,K})}$$

$$f^L = \begin{cases} 0 & f^{L,update} \leq 0 \\ f^{L,update} & 0 < f^{L,update} < \frac{y_{NO_x,0}}{y_{NO_x,0} - y_{NO_x,K}} \\ \frac{y_{NO_x,0}}{y_{NO_x,0} - y_{NO_x,K}} & f^{L,update} \geq \frac{y_{NO_x,0}}{y_{NO_x,0} - y_{NO_x,K}} \end{cases}$$

$$10 \quad y_{NH_3,k}^L = y_{L,NH_3} + f^L \cdot f_{NH_3,k} \cdot (y_{NO_x,k} - y_{NO_x,K})$$

$$y_{NO_x,k}^L = y_{NO_x,0} - f^L \cdot (y_{NO_x,0} - y_{NO_x,K})$$

$$\theta_{NH_3,k}^L = \frac{k_1(T_{s,k}) \cdot c_{tot,k} \cdot y_{NH_3,k}^L \cdot \eta_{NH_3,k}}{k_1(T_{s,k}) \cdot c_{tot,k} \cdot y_{NH_3,k}^L \cdot \eta_{NH_3,k} + k_2(T_{s,k}) + v_3 \cdot k_3(T_{s,k}) \cdot c_{tot,k} \cdot y_{NO_x,k}^L \cdot \eta_{NO_x,k}}$$

- 15 In the above formulae, y_{L,NH_3} is the permissible limit value for the mole fraction of ammonia after the catalyst, $T_{s,k}$ and $c_{tot,k}$ respectively are the catalyst temperature and the total gas concentration in channel segment k, v_3 is the stoichiometric coefficient for ammonia in the NO_x reduction reaction, and f^L is a capacity factor which describes the ratio between NO_x conversion at the catalyst's capacity limit and current NO_x conversion. The calculation converges quickly and four iterations are sufficient.
- 20 An iteration factor f^i is used for stabilising the calculation, and suitable values for this iteration factor in iterations two to four are
- 25 $f^2=0.2$, $f^3=0.1$ and $f^4=0$.

- The resulting limit value profile $\theta_{NH_3,k}^L$ for ammonia accumulation along the catalyst can thereafter be used in regulating in order to determine the NO_x conversion capacity of the catalyst under current operating conditions. This capacity is taken into account in calculating the accumulation setpoint value A2. Examples of conceivable formulae for determining the accumulation actual value A1 and the accumulation setpoint value A2 when implementing the embodiment according to Fig. 9 appear below.
- In this case the accumulation actual value A1 is calculated from the NO_x conversion in the first wall segment in all the channel segments along the catalyst, converted to an ammonia accumulation in the first wall segment of the first channel segment, according to the following formula:

$$A1 = \Phi_{NH_3} = \frac{\sum_{k=1}^K k_3(T_{s,k}) \cdot c_{tot,k} \cdot y_{NO_x,k} \cdot \eta_{NO_x,k} \cdot \theta_{NH_3,k}^L \cdot w_k}{k_3(T_{s,1}) \cdot c_{tot,1} \cdot y_{NO_x,1} \cdot \eta_{NO_x,1} \cdot w_1}$$

where w_k is the mass of active catalyst material in channel segment k. In the formula set out above, the numerator provides a measure of the catalyst's current NO_x.

The accumulation setpoint value A2 is obtained by an analogous calculation using the limit value profile $\theta_{NH_3,k}^L$ for the ammonia accumulation:

$$A2 = \Phi_{SP,NH_3} = f_{SP} \frac{\sum_{k=1}^K k_3(T_{s,k}) \cdot c_{tot,k} \cdot y_{NO_x,k} \cdot \eta_{NO_x,k} \cdot \theta_{NH_3,k}^L \cdot w_k}{k_3(T_{s,1}) \cdot c_{tot,1} \cdot y_{NO_x,1} \cdot \eta_{NO_x,1} \cdot w_1}$$

In the above formula, the numerator provides a measure of the catalyst's NOx conversion capacity under prevailing operating conditions.

The invention is of course in no way limited to the preferred embodiments described above, since a multiplicity of possibilities for modifications thereof are likely to be obvious to a specialist in the field without having thereby to deviate from the basic concept

5 of the invention such as it is defined in the attached claims. The exhaust system may for example comprise at least one additional catalyst connected in series with the reduction catalyst 4, e.g. an oxidation catalyst and/or a hydrolysis catalyst upstream from the reduction catalyst and/or a slip catalyst downstream from the

10 reduction catalyst.